

## The Department of Mathematics

2024–25–B term

**Course Name** O-minimality: topology without pathologies

**Course Number** 201.2.6141

**Course web page**

<https://math.bgu.ac.il/en/teaching/spring2025/courses/o-minimality-topology-wit>

**Lecturer** Prof. Assaf Hasson, <hassonas@bgu.ac.il>, Office 204

**Office Hours** <https://math.bgu.ac.il/en/teaching/hours>

### Abstract

### Requirements and grading<sup>1</sup>

### Course topics

In the 1980s A. Grothendieck suggest a project for developing a tame topology that will not suffer from the many counter-examples and pathologies known in classical topology. Nowadays many view the notion of o-minimality as successful fulfillment of this program: in o-minimal fields all (unary) functions are piecewise differentiable (and therefore infinitely differentiable at almost every point); unary functions are piecewise monotone, connectedness is the same as path connectedness and the axiom of choice holds for definable sets. In the o-minimal setting most of the classical differential calculus can be developed, and so are large portion of the theory of Lie groups, algebraic topology and much more. O-minimality plays a key role in real geometry and in recent years had a crucial role in important breakthroughs in Diophantine geometry and in Hodge theory. In the course we will define o-minimality and develop its basic theory. We will show that real closed fields are o-minimal and discuss – time permitting – some applications.

---

<sup>1</sup>Information may change during the first two weeks of the term. Please consult the webpage for updates