

## The Department of Mathematics

2021–22–B term

**Course Name** Introduction to representation theory of groups

**Course Number** 201.1.0511

**Course web page**

<https://math.bgu.ac.il/en/teaching/spring2022/courses/representation-theory>

**Lecturer** Dr. Inna Entova-Aizenbud, <entova@bgu.ac.il>, Office 312

**Office Hours** <https://math.bgu.ac.il/en/teaching/hours>

### Abstract

### Requirements and grading<sup>1</sup>

### Course topics

- .1 Introduction: Actions of groups on sets. Induced linear actions. Multilinear algebra.
- .2 Representations of groups, direct sum. Irreducible representations, semi-simple representations. Schur's lemma. Irreducible representations of finite abelian groups. Complete reducibility, Maschke's theorem.
- .3 Equivalent representations. Morphisms between representations. The category of representations of a finite group. A description using the group ring. Multilinear algebra of representations: dual representation, tensor product (inner and outer).
- .4 Decomposition of the regular representation into irreducible representations. The number of irreducibles is equal to the number of conjugacy classes. Matrix coefficients, characters, orthogonality.
- .5 Harmonic analysis: Fourier transform on finite groups and the non-commutative Fourier transform.
- .6 Frobenius divisibility and Burnside  $p^a q^b$  theorem.

---

<sup>1</sup>Information may change during the first two weeks of the term. Please consult the webpage for updates



- .7 Constructions of representations: induced representations. Frobenius reciprocity. The character of induced representation. Mackey's formula. Mackey's method for representations of semi-direct products.
- .8 Induction functor: as adjoint to restrictions, relation to tensor product. Restriction problems, multiplicity problems, Gelfand pairs and relative representation theory.
- .9 Examples of representations of specific groups:  $SL_2$  over finite fields, Icosahedron group, Symmetric groups.
- .10 Artin and Brauer Theorems on monomial representations