

Department of Mathematics, BGU

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# AGNT

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*On Wednesday, November 6, 2024*

*At 14:10 – 15:10*

*In 101-*

Nadav Gropper (University of Haifa)

will talk about

## **TQFTs for pro- $p$ Poincaré duality groups**

**Abstract:** In the talk, I will discuss the Turner-Turaev formalism for unoriented Topological Quantum Field Theory (TQFT). Building upon this formalism, I will introduce an analogous version for  $(d+1)$ -dimensional TQFT for pro- $p$  Poincaré duality groups. In the case of  $d = 1$ , this enables us to study cobordisms and TQFTs for both the maximal pro- $p$  quotient of absolute Galois groups of  $p$ -adic fields and  $\pi_1(X)^p$ , the pro- $p$  completions of fundamental groups of surfaces. This generalisation gives a framework for arithmetic TQFTs and strengthens the analogies within arithmetic topology, which relates  $p$ -adic fields to surfaces (oriented mod  $p^r$ ). I will explain the classification of TQFTs for the  $(1+1)$ -dimensional case, in terms of Frobenius algebras with some extra structure.

If time permits, I will explain how we define a Dijkgraaf-Witten like theory, to get formulas for counting  $G$ -covers of  $X$ , where  $X$  is either a surface, or a  $p$ -adic field, and  $G$  is a  $p$ -group (these formulas are similar to the ones given by Mednykh for surfaces using TQFTs, and by Masakazu Yamagishi using a more

algebraic approach). I will also try to outline how we plan to also get similar formulas for  $\text{Hom}(\pi_1(X)^p, G)$ , where  $G = \text{GL}_n(k)$  for  $k = \mathbb{F}_{p^r}$  or  $\mathbb{Z}/p^r\mathbb{Z}$ .

The talk is based on joint work with Oren Ben-Bassat.