Department of Mathematics, BGU

BGU Probability and Ergodic Theory (PET) seminar

On Tuesday, November, 7 2017

At 11:00 – 12:00

In 201

Michael Lin (BGU)

will talk about

Markov Operators

Abstract: This is the second survey talk in the series. See attached file.

MARKOV OPERATORS

MICHAEL LIN

ABSTRACT A transition probability on a measurable space (S, Σ) is a function $P: S \times \Sigma \longrightarrow [0, 1]$ satisfying:

(i) For fixed $s \in S$, $P(s, \cdot)$ is a probability on Σ .

(ii) For fixed $A \in \Sigma$, $P(\cdot, A)$ is measurable.

A transition probability defines the Markov operator $Pf(s) := \int f(t)P(s, dt)$ on bounded measurable functions, and the operator $\mu P(A) := \int P(s, A)d\mu(s)$ on finite signed measures on Σ . These are in duality: $\langle \mu P, f \rangle = \langle \mu, Pf \rangle$.

I will discuss some examples, explain how we obtain abstract Markov operators on $L_{\infty}(S, \Sigma, m)$, and describe some elements of the ergodic theory of L_1 contractions. The notions of ergodicity, weak mixing, mixing and complete mixing will be explained with relation to the general ergodic theorems, and the role of invariant probabilities $\mu P = \mu$ will be shown.

I will then describe the construction of the space of trajectories (Ω, \mathcal{B}) and the Markov chain generated by P.

DEPARTMENT OF MATHEMATICS, BEN-GURION UNIVERSITY, BEER-SHEVA, ISRAEL *E-mail address*: lin@math.bgu.ac.il